

SYBSCIT sem III Reg & A.T.K.T. Exam Oct-2022

S.Y.B.Sc.(IT) SEM-III

APPLIED MATHEMATICS

10/10/22



Duration: 2 hours & 30 Minutes

Total Marks : 75

NOTE:

- (i) All the questions are compulsory.
- (ii) All the questions carry equal marks.
- (iii) Simple calculator is allowed.

Q-1 Attempt Any Three:

[15]

[1] Verify Cayley-Hamilton Theorem for the matrix A. Given that;

$$A = \begin{bmatrix} 1 & 2 & -2 \\ -1 & 3 & 0 \\ 0 & -2 & 1 \end{bmatrix}; A^2 = \begin{bmatrix} -1 & 12 & -4 \\ -4 & 7 & 2 \\ 2 & -8 & 1 \end{bmatrix}; A^3 = \begin{bmatrix} -13 & 42 & -2 \\ -11 & 9 & 10 \\ -10 & -22 & -3 \end{bmatrix}$$

[2] Find Eigen Value of the matrix  $A = \begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$

[3] P.T. the following matrix is orthogonal and hence find  $A^{-1}$ .

$$A = \frac{1}{3} \begin{bmatrix} -2 & 1 & 2 \\ 2 & 2 & 1 \\ 1 & -2 & 2 \end{bmatrix}$$

[4] Find the Modulus and argument of: (a)  $1+i$  (b)  $1-\sqrt{3}i$

[5] Write in the form of  $r(\cos\theta + isin\theta)$ : (i)  $-1+i\sqrt{3}$  (ii)  $\sqrt{3} + i$

[6] Do as directed:

(i) Write  $\frac{3+2i}{2-3i}$  in standard form  $x + iy$ .

(ii) Write  $e^{i\theta}$  in the polar form.

(iii) Write the De Moivre's Theorem.

Q-2 Attempt Any Three:

[15]

[1] Solve:  $(x+1)\frac{dy}{dx} = x(y^2+1)$

[2] Solve:  $(xy^2+x)dx + (yx^2+y)dy = 0$

[3] Solve:  $(5x^4 + 3x^2y^2 - 2xy^3)dx + (2x^3y - 3x^2y^2 - 5y^4)dy = 0$

[4] Solve:  $(y^2 - x^2)dx + 2xydy = 0$

[5] Write the order and Degree of the following differential equations:

(i)  $\frac{d^2y}{dx^2} + ax^3 = 0$  (ii)  $x^2 \left(\frac{d^2y}{dx^2}\right)^2 + y \left(\frac{dy}{dx}\right)^3 + y^3 = 0$

[6] Solve:  $(D^2 + 4)y = \cos 2x$

[2]

**Q-3 Attempt Any Three:**

[15]

[1] Find  $L^{-1} \left[ \frac{2}{s} + \frac{1}{s^2} + \frac{s}{s^2-9} \right]$

[2] Find  $L^{-1} \left( \frac{s}{s^2-16} \right)$

[3] Find  $L^{-1} \left[ \frac{1}{s(s+a)} \right]$  by using convolution theorem.

[4] Find  $L[4t^2 + \sin 5t + e^{3t}]$

[5] Find  $L[e^{-3t} \cos 4t]$

[6] Find the Laplace/inverse Laplace transform of the following:

1.  $L(1)$  2.  $L[\cos x]$  3.  $L^{-1} \left( \frac{1}{s^4} \right)$  4.  $L^{-1} \left( \frac{1}{s+2} \right)$  5.  $L^{-1} \left( \frac{1}{s^2+2} \right)$

**Q-4 Attempt Any Three:**

[15]

[1] Evaluate:  $\int_0^3 \int_0^1 (x^2 + 3y^2) dy dx$

[2] P.T.  $\int_1^a \int_1^b \frac{1}{xy} dy dx = (\log a)(\log b)$

[3] Evaluate:  $\int_1^2 \int_1^3 xy^2 dx dy$

[4] Evaluate:  $\int_0^1 \int_0^2 \int_1^2 x^2 yz dz dy dx$

[5] Evaluate:  $\int_{-3}^3 \int_0^1 \int_1^2 (x + y + z) dx dy dz$

[6] Evaluate:  $\int_0^1 \int_{y^2}^1 \int_0^{1-x} x dz dy dx$

**Q-5 Attempt Any Three:**

[15]

[1] P.T.  $\beta(m, n) = \beta(m, n+1) + \beta(m, n+1)$

[2] Evaluate  $\int_0^\infty t^{\frac{3}{2}} e^{-t} dt$

[3] Evaluate:  $\int_0^\pi \sin^4 \theta d\theta$

[4] Evaluate  $\int_0^1 x^{\frac{3}{2}} (1-x)^{-\frac{5}{2}} dx$

[5] Evaluate  $\int_0^\pi \sin^3 \theta \cos^8 \theta d\theta$

[6] Evaluate:  $\int_0^\pi \cos^3 \theta d\theta$